

Spin Gap in the Zigzag Spin-1/2 Chain Cuprate $\text{Sr}_{0.9}\text{Ca}_{0.1}\text{CuO}_2$

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We report a comparative study of ^{63}Cu Nuclear Magnetic Resonance spin lattice relaxation rates, T_1^{-1} , on undoped SrCuO_2 and Ca-doped $\text{Sr}_{0.9}\text{Ca}_{0.1}\text{CuO}_2$ spin chain compounds. A temperature independent T_1^{-1} is observed for SrCuO_2 as expected for an $S = 1/2$ Heisenberg chain. Surprisingly, we observe an exponential decrease of T_1^{-1} for $T < 90\text{ K}$ in the Ca-doped sample evidencing the opening of a spin gap. The data analysis within the J_1 - J_2 Heisenberg model employing density-matrix renormalization group calculations suggests an impurity driven small alternation of the J_2 -exchange coupling as a possible cause of the spin gap.

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One-dimensional (1D) quantum magnets are intriguing model systems for studying correlated many-body quantum physics. They are theoretically well treatable which often yields clear-cut predictions about their ground states and excitation spectra (see, e.g., [1]). A particularly important case is the exactly solvable uniform antiferromagnetic (AFM) $S = 1/2$ Heisenberg chain model (HM) which exhibits a *gapless* spectrum of elementary spinon excitations and a ground state lacking long-range magnetic order. Spin gaps in the excitation spectra of closely related quantum systems arise only under certain circumstances. For instance they occur naturally in systems with a pronounced chemically caused dimerized structure or in spin-Peierls compounds with a spontaneously dimerized ground state [2, 3]. The latter become highly nontrivial in the presence of frustrated exchange interactions, being therefore a hot topic in the field of quantum magnetism. The parent compound SrCuO_2 considered here, where Cu^{2+} ($3d^9$, $S = 1/2$) ions bridged via oxygen ligands form well defined chain units along the crystallographic c -direction (see inset of Fig. 1), however, does not belong to either of them. It is commonly considered as one of the best realizations of the 1D $S = 1/2$ AFM HM. Due to a very small and frustrated coupling between different zigzag chains it shows a Néel-like ordering below $T_N \approx 2\text{ K}$ [7] only, despite the huge effective AFM next nearest neighbor (NNN) exchange integral $J_2 \sim 2000\text{ K}$ [4–6]. The nearest neighbor (NN) coupling J_1 is much weaker, ferromagnetic (FM) and frustrated with an estimated ratio of $|J_1/J_2| \lesssim 0.1 - 0.2$ [8]. Inelastic neutron scattering reports the onset of a weak sublattice magnetization below $T_{c1} = 5\text{ K}$, static on a ns time scale, but the absence of 3D long range order for $T \gtrsim 10^{-4}J/k_B$. Furthermore, it suggests a gapless spinon excitation spectrum for this compound down to the lowest measured energy transfer of 0.5 meV [9]. However, despite inevitably present spin-phonon coupling, a spin-Peierls transition has not been found at low temperature, in contrast to the well-known CuGeO_3 [10].

In this Letter we address this dichotomy by studying the effect of isovalent Ca substitution on the Sr sites in

SrCuO_2 , outside the spin chain unit. Our comparative Nuclear Magnetic Resonance (NMR) study investigates the temperature dependence of the ^{63}Cu nuclear spin lattice relaxation rate T_1^{-1} for single crystals of SrCuO_2 and $\text{Sr}_{0.9}\text{Ca}_{0.1}\text{CuO}_2$. While T_1^{-1} is temperature independent in SrCuO_2 in compliance with the $S=1/2$ HM and the observed gapless spinon continuum [9], an exponential decrease of T_1^{-1} below 90 K for $\text{Sr}_{0.9}\text{Ca}_{0.1}\text{CuO}_2$ evidences a significant gap in the spin excitation spectrum. We present a theoretical analysis of this striking observation in terms of the J_1 - J_2 1D HM for two possible scenarios: (i) the AFM-AFM frustrated HM for which, based on qualitative arguments only, a small spin gap has been predicted in the crossover region between a commensurate dimerized-like and an incommensurate spiral-like state [11]; (ii) the standard spin-Peierls scenario with an alternation of the largest AFM NNN coupling J_2 in the presence of a realistic relatively small NN coupling J_1 of arbitrary sign. We conclude on the relevance of scenario (ii) for the occurrence of a spin gap in $\text{Sr}_{0.9}\text{Ca}_{0.1}\text{CuO}_2$ where subtle structural distortions due to Ca substitution might cause a small modulation of J_2 and trigger a drastic change of the spin excitation spectrum.

Single crystals of SrCuO_2 and $\text{Sr}_{0.9}\text{Ca}_{0.1}\text{CuO}_2$ were grown by the travelling solvent floating zone method. Their high quality, i.e. single crystallinity, stoichiometry, the absence of phase irregularities, and second phase inclusions, was verified by x-ray diffraction, polarized optical microscopy, energy-dispersive x-ray spectroscopy and inductively coupled plasma optical emission spectrometry [12]. The Ca-content of $\text{Sr}_{0.9}\text{Ca}_{0.1}\text{CuO}_2$ was found to be $(10.0 \pm 0.2)\%$. Structural refinement on $\text{Sr}_{0.9}\text{Ca}_{0.1}\text{CuO}_2$ showed no measurable Ca occupancy of the Cu sites. The averaged change of the Cu-O-Cu bond angle and bond distance along the direction of J_2 is only 0.35% . The ^{63}Cu NMR spin lattice relaxation rate, T_1^{-1} , was measured by inversion recovery in a magnetic field of $H = 7.0494\text{ T}$ for $H \parallel a$, b and c , respectively. The values of T_1^{-1} were obtained by fitting the recovery curves to the standard expression for magnetic relaxation of a nuclear spin $I = 3/2$ [13, 14] yielding one single T_1 component

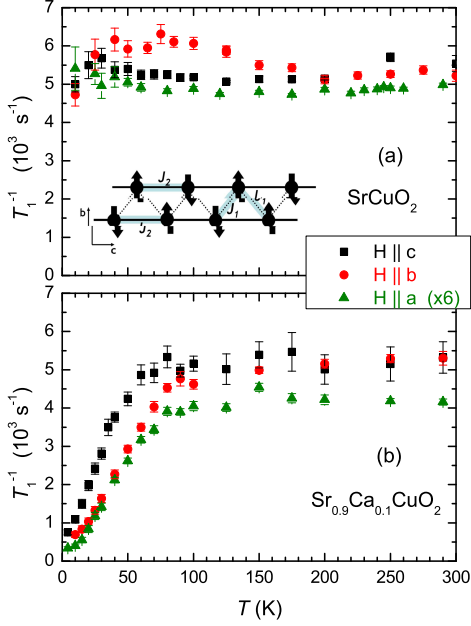


FIG. 1: (color online) Spin lattice relaxation rate T_1^{-1} of SrCuO_2 (a) and $\text{Sr}_{0.9}\text{Ca}_{0.1}\text{CuO}_2$ (b) for different field directions. Inset: zigzag structure and main couplings.

at any temperature [15].

For SrCuO_2 , T_1^{-1} remains constant over the whole temperature range, and increases only slightly at low temperature [Fig. 1(a)] [16]. Note that the error bars increase with decreasing temperature due to a strong broadening of the NMR resonance lines at low temperature [17]. The observed behavior strongly supports the gapless excitation spectrum in SrCuO_2 and is consistent with theoretical calculations for the $S=1/2$ AFM HM predicting a temperature independent T_1^{-1} [18–20]. Fig. 1(b) shows the temperature dependence of T_1^{-1} for $\text{Sr}_{0.9}\text{Ca}_{0.1}\text{CuO}_2$. Similar to the undoped sample, T_1^{-1} shows the expected temperature independent behavior for $T > 90$ K, but unexpectedly decreases exponentially by more than one order of magnitude for $T < 90$ K [21].

In case of magnetic relaxation the spin lattice relaxation rate probes directly the imaginary part of the dynamic susceptibility χ'' of the electronic spin system:

$$T_1^{-1} \propto \frac{T}{\text{const.}} \sum_{\vec{q}} A_{\perp}^2(\vec{q}, \omega) \cdot \frac{\chi''(\vec{q}, \omega)}{\omega}. \quad (1)$$

Here A_{\perp} is the hyperfine coupling, \vec{q} the wave vector and ω the NMR frequency. The observed exponential decrease of T_1^{-1} gives therefore evidence for the opening of a gap Δ in the excitation spectrum of $\text{Sr}_{0.9}\text{Ca}_{0.1}\text{CuO}_2$ that is manifested by an exponential reduction of χ'' . We estimated the magnitude of the gap by fitting our data to an activated temperature dependence:

$$T_1^{-1}(T) = T_{1,\text{off}}^{-1} + \text{const.} \cdot e^{(-\Delta/T)}, \quad (2)$$

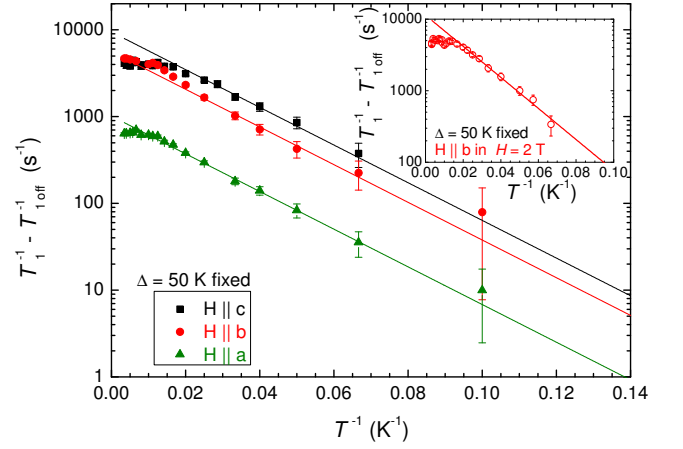


FIG. 2: (Color online) Spin lattice relaxation rate T_1^{-1} of $\text{Sr}_{0.9}\text{Ca}_{0.1}\text{CuO}_2$ vs. inverse temperature. Lines are fits of Eq. (2) with a fixed spin gap of $\Delta = 50$ K at low temperature (10 - 40 K). For clarity $T_{1,\text{off}}^{-1}$ has been subtracted from the data and the fits. Inset: the same for $H \parallel b$ in $H = 2$ T.

which applies for $T < \Delta$. To account for the non-vanishing value of T_1^{-1} as $T \rightarrow 0$, we added a constant offset $T_{1,\text{off}}^{-1}$ to the activation behavior. The results shown in Fig. 2 clearly demonstrate that for $T \leq 40$ K the decrease of T_1^{-1} can be well described with an isotropic spin gap of $\Delta = 50$ K. A possible field dependence could be excluded by supplementary measurements of T_1^{-1} in $H = 2$ T, also yielding $\Delta = 50$ K (see inset of Fig. 2).

The opening of a spin gap suggests that the magnetic properties of the Cu spin chains change drastically by substituting Sr with isovalent Ca. Note that neither in susceptibility nor in other thermodynamic properties any indication for a spin gap was found. This is not surprising since owing to the very large value of J_2 the intrinsic static magnetic susceptibility at $T \ll J_2$ is very small. Therefore the thermodynamics might just overlook the gap since the total static magnetic response at low T is dominated by other contributions, such as the Van-Vleck susceptibility and Curie-like impurity contributions.

Two different approaches to explain such a doping-induced spin gap in $\text{Sr}_{0.9}\text{Ca}_{0.1}\text{CuO}_2$ will be discussed based on the following spin Hamiltonian written in the adiabatic approximation:

$$H = J_1 \sum_i \vec{S}_i \cdot \vec{S}_{i+1} + J_2 \sum_i (1 + (-1)^\alpha \delta) \vec{S}_i \cdot \vec{S}_{i+2}. \quad (3)$$

Here \vec{S}_i is a spin- $\frac{1}{2}$ operator at site i and $\alpha = \sqrt{2} \sin \frac{\pi}{4} (2i - 1)$, J_1 and J_2 are the NN and the NNN exchange interactions and δ is the modulation of J_2 . The spin gap is evaluated as the energy difference between the lowest triplet state and the singlet ground state,

$$\Delta(L) = E_1(L) - E_0(L), \quad \Delta = \lim_{L \rightarrow \infty} \Delta(L), \quad (4)$$

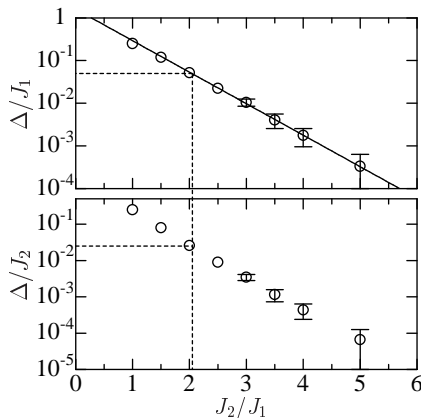


FIG. 3: Spin gap as a function of J_2/J_1 in the AFM-AFM sector of the J_1 - J_2 HM. The experimental value of the spin gap in units of J_1 is depicted by dashed lines adopting $J_2 = 2000$ K.

where $E_n(L)$ is the n -th eigenenergy ($n = 0$ denotes the ground state) of the system with length L . We employ the density-matrix renormalization group (DMRG) technique, a powerful numerical method for various 1D quantum systems [22]. Open-end boundary conditions are applied in the chain direction and it enables us to calculate the energies of the ground-state and low-lying excited-states quite accurately for very large but always finite systems (up to the order of $\sim 10^3$ sites).

Scenario (i) gives attention to the frustrated NN coupling J_1 . For FM NN interaction $J_1 < 0$, whose absolute value is much smaller than the NNN interaction J_2 , as it is likely the case in SrCuO_2 , the zigzag chain is not expected to show a spin gap [11]. However, in the case of a small AFM NN coupling $J_1 > 0$, the zigzag chain should exhibit a spin gap which scales exponentially with the ratio of the two competing couplings [11]:

$$\Delta \propto \exp\left(-\text{const.} \cdot \frac{J_2}{J_1}\right). \quad (5)$$

According to the Goodenough-Kanamori-Anderson (GKA) rules [23] a Cu-O-Cu bond angle of 180° yields a strong AFM exchange between the Cu spins (J_2), while an angle of 90° results in a weak FM coupling (J_1). However, as soon as the bond angle slightly deviates from 90° , the interaction J_1 can become AFM again [24]. Local structural distortions in $\text{Sr}_{0.9}\text{Ca}_{0.1}\text{CuO}_2$ induced by Ca ions could yield such a deviation, resulting in a local spin gap corresponding to Eq. (5).

Within this scenario ($\delta = 0$ and $J_1 > 0$) we study chains with several lengths $L = 512$ to 4096 , keeping $m = 1200$ density-matrix eigenstates in the renormalization procedure. In this way, the discarded weight, w_d , is less than 10^{-7} , while the maximum error ΔE in the ground-state and low-lying excited states energies is less than $10^{-7} - 10^{-6}$. The extrapolated results of the spin gap are shown in Fig. 3. For $J_2/J_1 \geq 2$, the spin gap can be

well fitted by the expression

$$\Delta/J_1 = 1.6 \exp(-1.7J_2/J_1), \quad (6)$$

which might be useful for the description of frustrated systems in general. However, for the zigzag chain under consideration with the experimentally obtained gap of $\Delta = 50$ K a value of $J_1 \sim 1000$ K would be required to explain our NMR data. This is unrealistically large for a Cu-O bond angle only slightly below or above 90° [24, 25]. Hence, scenario (i) can be discarded.

Scenario (ii) examines the possibility of an alternating AFM NNN exchange $J_2(1 \pm \delta)$, which is known to cause an intrinsic spin gap. Within this scenario we assume that the Ca substitution might induce either directly or via a softening of the lattice and a concomitant strongly increased spin-phonon interaction a modulation of the NNN coupling constant J_2 , whose simplest realization is a periodic alternation. The validity of this scenario will be examined for FM and AFM J_1 .

We study chains with several lengths $L = 64$ to 392 , keeping $m = 2000$, which ensures $w_d < 10^{-14}$ and $\Delta E < 10^{-12}$. In Fig. 4(a), the spin gap is plotted as a function of δ for $J_1 = 0$. We estimate $\delta = 0.0027$ to reproduce the experimental value of the spin gap $\Delta = 50$ K for $J_2 = 2000$ K. Next, we introduce the NN exchange interaction J_1 . The spin gap is calculated as a function of J_1 with fixed $\delta = 0.0027$ [Fig. 4(b)]. We find that the value of Δ is hardly affected by J_1 . Thus, only a small alternation factor $\delta = 0.0027$ is needed to reproduce the spin gap found by NMR, irrespective of the strength and sign of the interchain coupling $|J_1| \ll J_2$.

Beyond the simple alternation of J_2 , a more realistic situation would be given by including also the direct impact of disorder in the exchange coupling caused by the Ca impurities. Thus, we consider an additional term to Eq. (3), $H_{\text{dis}} = 2D \sum_{i=1}^{L-2} \varepsilon_i \vec{S}_i \cdot \vec{S}_{i+2}$, where ε_i is defined by a box probability distribution $\mathcal{P}(\varepsilon_i) = \theta(1/2 - |\varepsilon_i|)$ with the step function $\theta(x)$ and the disorder strength is controlled by D . We calculate the spin structure factor $S(q = \pi, \omega)$ on random sampling 30 realizations of $\mathcal{P}(\varepsilon_i)$ for $L = 384$, using dynamical DMRG [26], and take an average of the results for each D . Fig. 4(c) shows the averaged $S(q = \pi, \omega)$ for several D values with $\delta = 0.1$ and $J_1 = 0$. We find that the delta peak for $D = 0$ is broadened by the disorder and a "pseudo spin gap"-like behavior appears. Note that a relatively large $\delta = 0.1$ is chosen to be able to clearly follow the D -dependence. For $D > \delta$ the singlet pairs are partially collapsed, i.e., magnetic moments are locally induced, and the spectral weight at $\omega = 0$ becomes finite. This must be related to the occurrence of a finite, doping-dependent residual relaxation rate $T_{1,\text{off}}^{-1}$ [see Eq. (2) and Fig. 1(b)].

In summary, measurements of the ^{63}Cu NMR spin lattice relaxation rate T_1^{-1} in a single crystal of the $S = 1/2$ chain compound $\text{Sr}_{0.9}\text{Ca}_{0.1}\text{CuO}_2$ reveal a striking exponential decay of T_1^{-1} below 90 K in sharp contrast to a

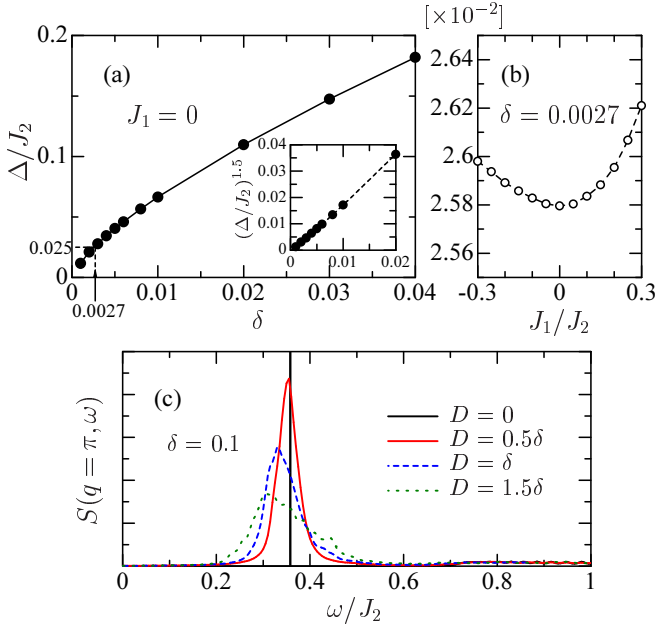


FIG. 4: The same as in Fig. 3 for an alternating AFM NNN exchange $J_2(1 \pm \delta)$ at (a) zero and (b) weak arbitrary NN-exchange J_1 . (c) Spin structure factor for several disorder strengths D with $\delta = 0.1$ and $J_1 = 0$. The inset of (a) shows $(\Delta/J_2)^{1.5}$ for small alterations δ .

constant T_1^{-1} in the parent compound SrCuO_2 [27]. The observed decay points to the opening of a spin gap with $\Delta = 50$ K. Our DMRG calculations show that this spin gap can be well reproduced within the J_1 - J_2 1D HM considering an alternating AFM NNN $J_2(1 \pm \delta)$ with only a small alternation of about $\delta = 0.0027$, regardless of the strength and sign of the NN J_1 . Such a remarkable sensitivity of the low energy excitation spectrum of the $S = 1/2$ chains in SrCuO_2 to structural substitutional defects outside the zigzag chain appears to be crucial for the understanding of the spin dynamics in low dimensional cuprates. Our results call therefore for extensive experimental and theoretical work on this and related systems to understand the impact of additional degrees of freedom on the fundamental magnetic phenomena occurring in quantum spin magnets on the basis of cuprates. For example diffraction experiments may confirm the dimerization [29], while neutron scattering, resonant inelastic x-ray spectroscopy, optics and specific heat may observe the spin gap and/or a possible phonon softening. So far there seem to be no generally accepted microscopic models for spin-Peierls physics in cuprates. We hope that our work will stimulate the development of such models.

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